



## Intervention analysis of Daily Brazilian Real / Nigerian Naira Exchange Rates Because of the 2020 Nigerian Recession

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### ABSTRACT

This paper is an attempt to model intervention between daily Brazilian real (BRL) and Nigerian naira (NGN) exchange rates. A look at the time plot of the exchange rates series shows that there is an intervention believed to have been caused by the announced economic recession of the year 2020 in Nigeria induced by the advent of covid-19 pandemic. The data are therefore from September 2020 to December 2020. It is clear that the exchange rates rose sharply from November 20 up to 31 December, 2020. The pre-intervention data are non-stationary. This necessitates its differencing; the first differences are now stationary. The correlogram of the differences shows an autocorrelation structure of a white noise process. Post-intervention forecasts of the model are each equal to the last pre-intervention rate of 72.2711. The transfer function of the model has been estimated and the fitted model has been shown to closely agree with the post-intervention data. This is a testimony to its adequacy. Pearson chi-square goodness-of-fit test confirms its adequacy. It may be found useful by planners and administrators.

**Keywords:** Brazilian real, Nigerian naira, exchange rates, intervention, 2020 Nigerian recession, covid-19

### INTRODUCTION

Brazilian real (BRL) is the legal tender of Brazil whereas the Naira (NGN) is that of Nigeria. Bilateral relations are on the basis of how much one currency goes for another. The year 2020 was phenomenal for Nigeria with the incident of covid-19 in February which brought about the Nigerian economic recession that year (Aljazeera, 2020). It is believed that the recession made the intervention happen. This is the basis of this work. The approach of intervention adopted is that of Box and Tiao (1975) who proposed the use of Box-Jenkins (1976) ARIMA modeling. A lot of authors have used this approach to solve intervention problems. These include Gilmour *et al.* (2006), Nkwocha (2019), Rosales-Lopez *et*

*a/.* (2018), Okereke *et al.*(2016), Oreko *et al.* (2017), Mrinmoy *et al.* (2014), Yaacob *et al.* (2011) and Jarrett and Kyper (2011). Etuk *et al.* (2021) studied the intervention witnessed of the BRL/NGN exchange rates as a result of the 2016 Nigerian recession.

## MATERIALS AND METHODS

### Data

The data for this work came from the website <https://www.exchangerates.org.uk/BRL-NGN-exchange-rates-history.html>. They are the daily BRL/NGN exchange rates from 1 September 2020 to 31 December 2020. They are to be read as the amount of NGN in one BRL.

### Intervention Analysis

The method adopted for this intervention analysis is the one proposed and demonstrated by Box and Tiao (1975). It was based on the autoregressive integrated moving average (ARIMA) modeling technique of Box and Jenkins (1976).

Suppose that  $X_1, X_2, \dots, X_n$  is a realization of a time series  $\{X_t\}$ . Let there be an intervention at  $t=T$  where  $T < n$ . Model the pre-intervention part of the series with an ARIMA model. Suppose the order of the ARIMA is  $(p, d, q)$ .

That means for  $t < T$

$$\nabla^d X_t = \alpha_1 \nabla^d X_{t-1} + \alpha_2 \nabla^d X_{t-2} + \dots + \alpha_p \nabla^d X_{t-p} + \dots + \varepsilon_t + \beta_1 \varepsilon_{t-1} + \beta_2 \varepsilon_{t-2} + \dots + \beta_q \varepsilon_{t-q} \dots \dots \dots (1)$$

That is,

$$\nabla^d (1 - \alpha_1 L - \alpha_2 L^2 - \dots - \alpha_p L^p) X_t = (1 + \beta_1 L + \beta_2 L^2 + \dots + \beta_q L^q) \varepsilon_t \dots \dots \dots (2)$$

where  $\{\varepsilon_t\}$  is a white noise series,  $\nabla$  is the difference operator and  $L$  is the backshift operator defined by  $LX_t = X_{t-1}$ .

The model (2) may be written as

$$\nabla^d \Phi(L) X_t = \Theta(L) \varepsilon_t \dots \dots \dots (3)$$

Whereby  $X_t = \frac{\Theta(L) \varepsilon_t}{\Phi(L) \nabla^d}$  is the noise part of the intervention model where  $\nabla = 1-L$ .



On the basis of this model make post-intervention forecasts  $f$ .

Let  $z = X_t - f$ ,  $t \geq T$ . Then

$$Z = c(1) * (1 - c(2) ^ (t-T+1)) / (1 - c(2)) \dots \dots \dots (4)$$

where  $c(1)$  and  $c(2)$  are constants.

Combining (3) and (4), the intervention model is

$$X_t = \frac{\Theta(L)\varepsilon_t}{\Phi(L)\nabla^d} + c(1) * \frac{(1-c(2)^{t-T+1}}{1-c(2)} \dots \dots \dots (5)$$

### Computer Software

Eviews 10 was used for computations in the work.

### RESULTS

In figure 1 is a time plot of the BRL/NGN exchange rates for the year 2020 beginning from 1 September 2020. There is an intervention at the close of the year as observable. This intervention is around November 2020 when the news of the economic recession in Nigeria was announced by the National Bureau of Statistics of Nigeria. This implies causality. Generally the trend is upward. Rather arbitrarily the intervention is taken for  $t=81$ , i.e. 20 November 2020.

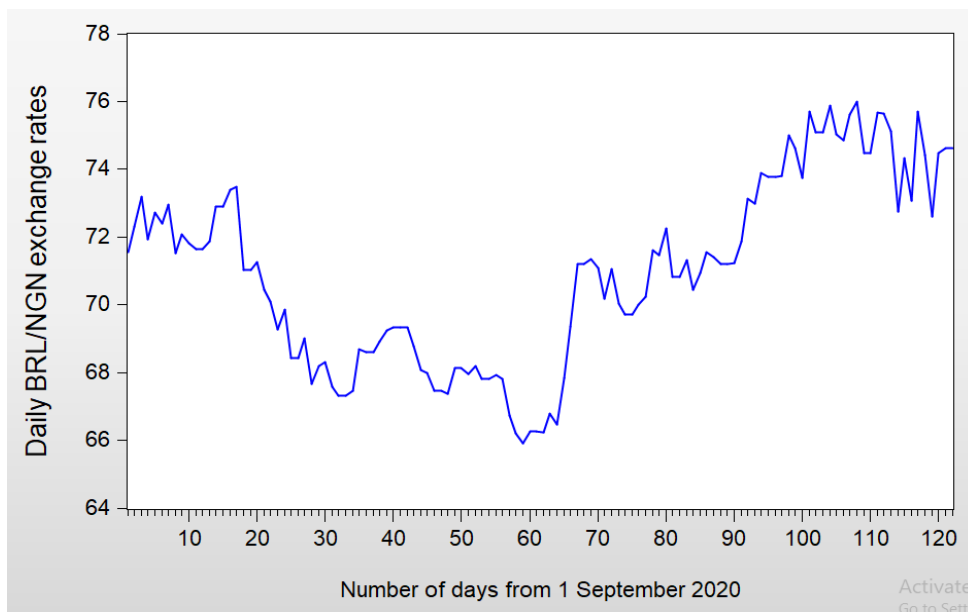


Figure 1: Time plot of the BRL/NGN exchange rates

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Figure 2 is the time plot of the pre-intervention series. There is a generally negative trend.

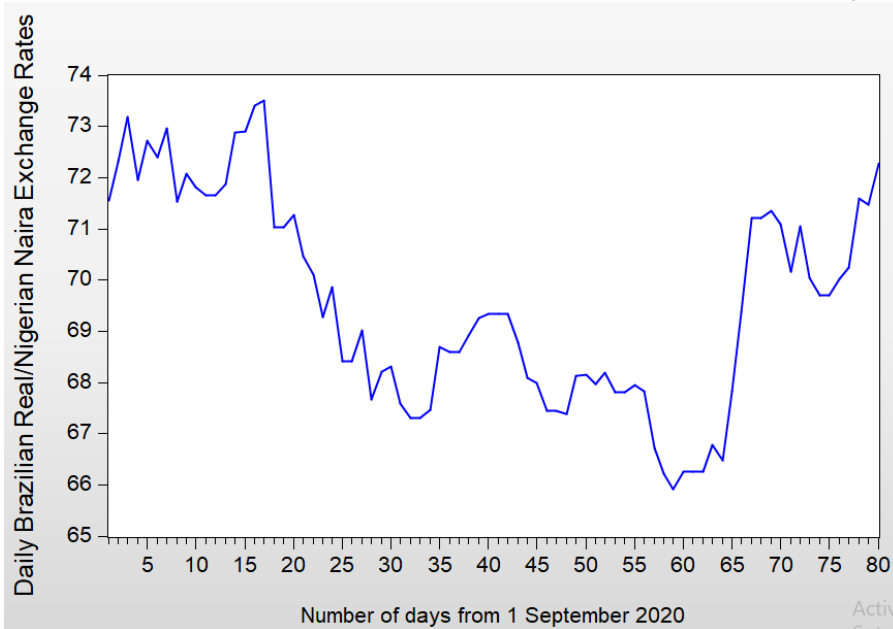


Figure 2: Time plot of the pre-intervention exchange rates

Table 1: Unit root test for the pre-intervention rates

Null Hypothesis: BRLN1 has a unit root  
 Exogenous: Constant, Linear Trend  
 Lag Length: 0 (Automatic - based on SIC, maxlag=11)

	t-Statistic	Prob.*
Augmented Dickey-Fuller test statistic	-0.890197	0.9515
Test critical values:		
1% level	-4.078420	
5% level	-3.467703	
10% level	-3.160627	

\*MacKinnon (1996) one-sided p-values.

Augmented Dickey-Fuller Test Equation  
 Dependent Variable: D(BRLN1)  
 Method: Least Squares  
 Date: 03/18/22 Time: 23:29  
 Sample (adjusted): 2 80  
 Included observations: 79 after adjustments

Variable	Coefficient	Std. Error	t-Statistic	Prob.
BRLN1(-1)	-0.039506	0.044379	-0.890197	0.3762
C	2.640303	3.165212	0.834163	0.4068
@TREND("1")	0.002894	0.003974	0.728198	0.4687
R-squared	0.031803	Mean dependent var		0.009053
Adjusted R-squared	0.006324	S.D. dependent var		0.711677
S.E. of regression	0.709423	Akaike info criterion		2.188506
Sum squared resid	38.24937	Schwarz criterion		2.278485
Log likelihood	-83.44597	Hannan-Quinn criter.		2.224554
F-statistic	1.248192	Durbin-Watson stat		2.009981
Prob(F-statistic)	0.292839			



Clearly from the Table 1 results the pre-intervention series are not stationary, the p-value being 0.95 much greater than 0.05. There is therefore the need for differencing of the series. Figure 3 is the time plot of the differenced series.

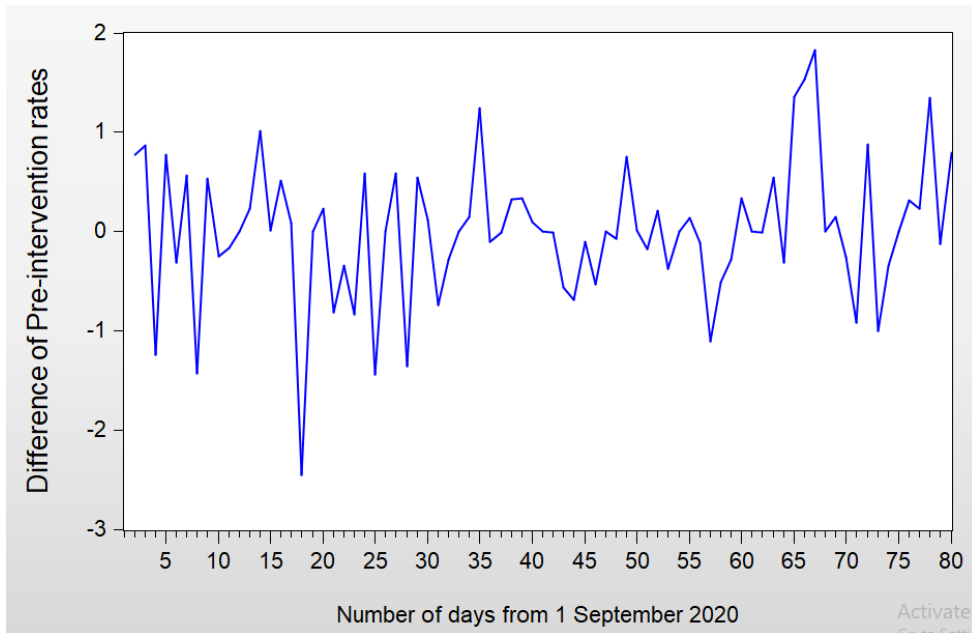


Figure 3: Time plot of the difference of the pre-intervention series

The result of Table 2 test shows that the difference series is stationary with a p-value of 0.0000 which is less than 0.05. The correlogram of the difference series in Figure 4 shows that all its spikes are within the non-significance range. This implies a white noise model for the difference series, which in turn implies a post-intervention forecast of 72.2711 for each post-intervention point. That is,  $f=72.2711$ .

Define  $z = \text{brl/ngn} - f, t > 80$

Table 2: Unit root test for the difference of the pre-intervention data

Null Hypothesis: DBRLN1 has a unit root

Exogenous: Constant

Lag Length: 0 (Automatic - based on SIC, maxlag=11)

	t-Statistic	Prob.*
Augmented Dickey-Fuller test statistic	-8.961894	0.0000
Test critical values:		
1% level	-3.516676	
5% level	-2.899115	
10% level	-2.586866	

\*MacKinnon (1996) one-sided p-values.

Augmented Dickey-Fuller Test Equation

Dependent Variable: D(DBRLN1)

Method: Least Squares

Date: 03/18/22 Time: 23:36

Sample (adjusted): 3 80

Included observations: 78 after adjustments

Variable	Coefficient	Std. Error	t-Statistic	Prob.
DBRLN1(-1)	-1.027958	0.114703	-8.961894	0.0000
C	-0.000763	0.080991	-0.009417	0.9925
R-squared	0.513804	Mean dependent var		0.000223
Adjusted R-squared	0.507407	S.D. dependent var		1.019153
S.E. of regression	0.715292	Akaike info criterion		2.193056
Sum squared resid	38.88488	Schwarz criterion		2.253484
Log likelihood	-83.52917	Hannan-Quinn criter.		2.217246
F-statistic	80.31555	Durbin-Watson stat		1.991065
Prob(F-statistic)	0.000000			

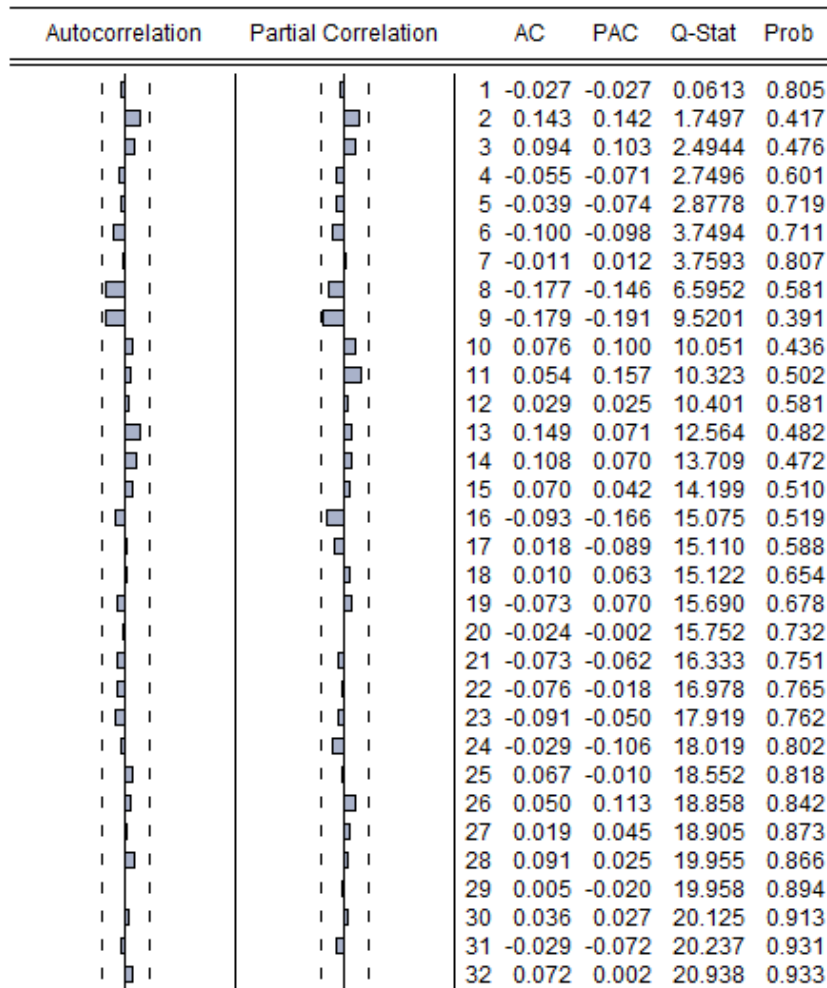


Figure 4: Correlogram of the difference of the pre-intervention data

This correlogram implies that the fit to the differences of the pre-intervention data is a white noise process. This means that the post-intervention forecasts on the basis of this are each equal to 72.2711, the value of the original series at the last pre-intervention date, that is, November 19, 2020.

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Table 3: Transfer function determination for the intervention model

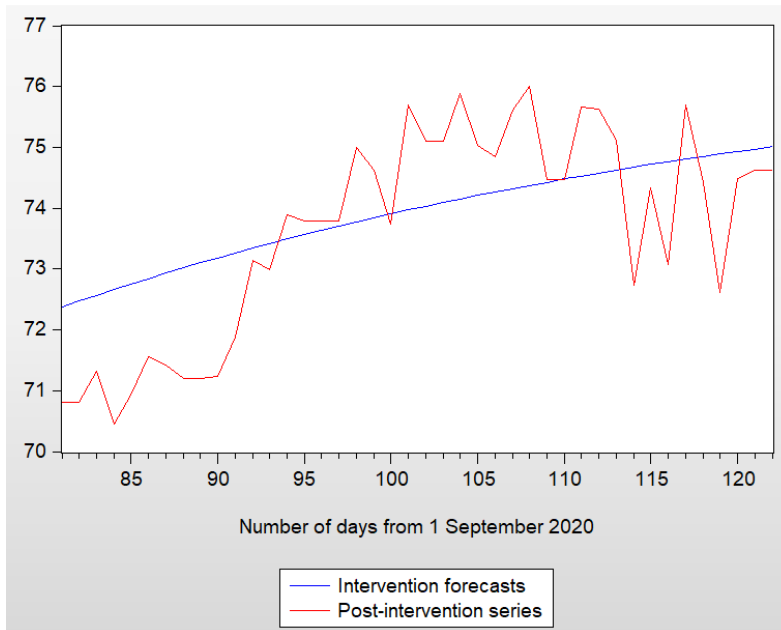
Dependent Variable: Z  
 Method: Least Squares (Gauss-Newton / Marquardt steps)  
 Date: 03/18/22 Time: 23:48  
 Sample: 81 122  
 Included observations: 42  
 Convergence achieved after 32 iterations  
 Coefficient covariance computed using outer product of gradients  
 $Z=C(1)*(1-C(2)^{(T-80))}/(1-C(2))$

	Coefficient	Std. Error	t-Statistic	Prob.
C(1)	0.101146	0.041418	2.442083	0.0191
C(2)	0.976955	0.030239	32.30732	0.0000
R-squared	0.472911	Mean dependent var		1.369645
Adjusted R-squared	0.459734	S.D. dependent var		1.715963
S.E. of regression	1.261281	Akaike info criterion		3.348580
Sum squared resid	63.63316	Schwarz criterion		3.431326
Log likelihood	-68.32018	Hannan-Quinn criter.		3.378910
Durbin-Watson stat	0.660682			

The intervention model is given by

$$X_t = \frac{0.101146(1-0.976955^{t-80})}{0.023045} + \frac{\varepsilon_t}{1-L} \quad (6)$$

by model (5).







The Pearson chi-square goodness-of-fit statistic is equal to  $0.7835 < \chi^2_{0.01} = 63.7$  meaning that the p-value  $< 0.01$ . This is a testimony to the goodness-of-fit of the intervention model to the post-intervention data.

## CONCLUSION

Adequacy of the intervention model (6) to the post-intervention data is not in doubt. This avails as model to use for planning purpose to seek redress of the situation, especially to the relatively suffering party. Coincidentally this year witnessed the advent of the covid-19 pandemic in this country at the present time. The study might be said to have been conducted during the time of influence of the pandemic in Nigeria. Administrators shall find the result of this study very useful.

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